## Functions

Function Notation:
A function can be thought of as a $\qquad$ that assigns
$\qquad$ to $\qquad$ .


Examples:

1. If $f(x)=3 x^{2}-4 x$, find the function value for:
a. $f(6)$
b. $f(x+2)$
2. If $f(x)=\left\{\begin{array}{c}|x+2|, x \leq 2 \\ \frac{2}{3} x-1,2<x \leq 6 \\ 3, x>6\end{array}\right.$
find the function value for:
a. $f(6)$
b. $f(0)$
3. If $f(x)=6$, find the function value for:
a. $f(-3)$
b. $f\left(x^{2}\right)$
4. Determine with the relation is a function:
a.

| $x$ | -1 | 2 | 5 |
| :---: | :---: | :---: | :---: |
| $y$ | -4 | 8 | 20 |

b.

c. $\{-1,5),(2,5),(3,5)(8,5)\}$

Function Operations:

## Operations with Functions

| Operations with Functions |  |
| :--- | :--- |
| $(f+g)(x)$ means $f(x)+g(x)$ <br> Example: $f(x)=3 x+5, g(x)=2 x-7$ | $(f-g)(x)$ means $f(x)-g(x)$ <br> Example: $: f(x)=2 x-4, g(x)=x+3$ |
| $(f \cdot g)(x)$ means $f(x) \cdot g(x)$ <br> Example: $: f(x)=x+2, g(x)=x-3$ | $\frac{f}{g}(x)$ means $\frac{f(x)}{g(x)}$ <br> Example: $: f(x)=x^{2}-16, g(x)=x+4$ |

Composition of functions:

Example: $\mathbf{f}(\mathbf{x})=\mathbf{2 x + 3}$ and $\mathbf{g}(\mathbf{x})=\mathbf{x}^{\mathbf{2}}$
" $x$ " is just a placeholder, and to avoid confusion let's just call it "input":

$$
\begin{aligned}
& f(\text { input })=2(\text { input })+3 \\
& g(\text { input })=(\text { input })^{2}
\end{aligned}
$$

So, let's start:

$$
(g \circ f)(x)=g(f(x))
$$

First we apply $f$, then apply $g$ to that result:


$$
\left(g^{0} f\right)(x)=(2 x+3)^{2}
$$

Examples: Let $f(x)=x^{2}, g(x)=\sqrt{x}+1, \mathrm{~h}(\mathrm{x})=2 \mathrm{x}+3$

1. $f o g(4)=f(g(4))=$
2. $g(h(x))=$
3. $f(h(x))=$

Inverse Relations: "switch the $x$ and $y$ ", if the inverse is a function then it is called an inverse function

Examples:

1. Find the inverse realation from the table:

| $\boldsymbol{x}$ | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | 3 | 5 | 7 | 9 | 11 |

Is the inverse a function?
3. Verify the $f$ and $g$ are inverses:

$$
f(x)=x+2 ; g(x)=x-2
$$

Rates of change: Simply means slope
Slope of any line by using the slope formula between 2 points.
"Average Rate of Change" Simply means draw a line through 2 points and find the slope.
Examples:

| 1. Find the average rate of change of $f(x)=x^{2}+3$ <br> on the interval $[0,2]$ | Find the average rate of change of $f(x)=3 x^{3}$ on <br> the interval $[-2,3]$ |
| :--- | :--- |

