

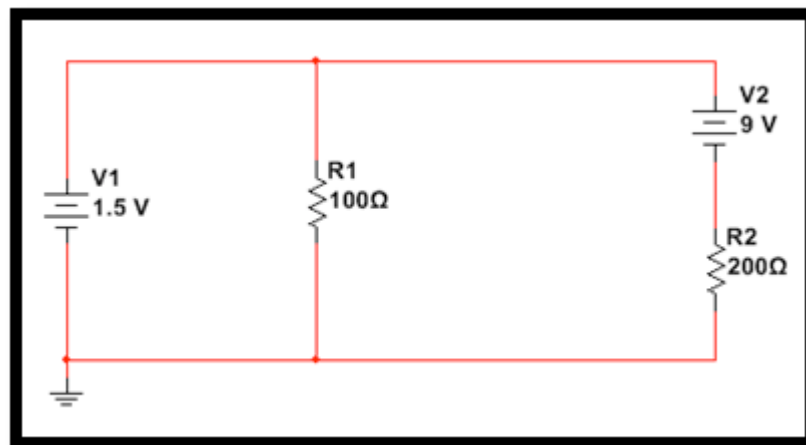
5.2 Kirchhoff's laws worksheet

Kirchhoff's Current Law - states that the current entering a point in a circuit is equal to the summation of the currents exiting.

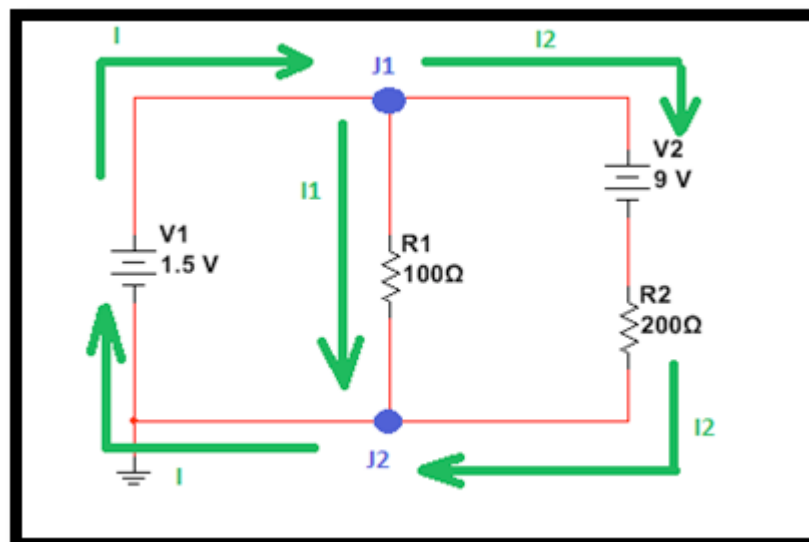
Kirchhoff's Voltage Law - states that the summation of all voltage drops in a closed loop must equal to zero which is a result of the electrostatic field being conservative.

(Conventional) current flowing through the cell has a positive voltage (gains energy). Current going through a resistor has a negative voltage (loses energy).

Example Problem



Begin by labelling the junctions in our circuit, J_1 and J_2 . Then we label the currents as I , I_1 and I_2 in an arbitrary direction as shown in the figure below. (Direction of currents will be confirmed once we complete the problem).



Junction J_1 :

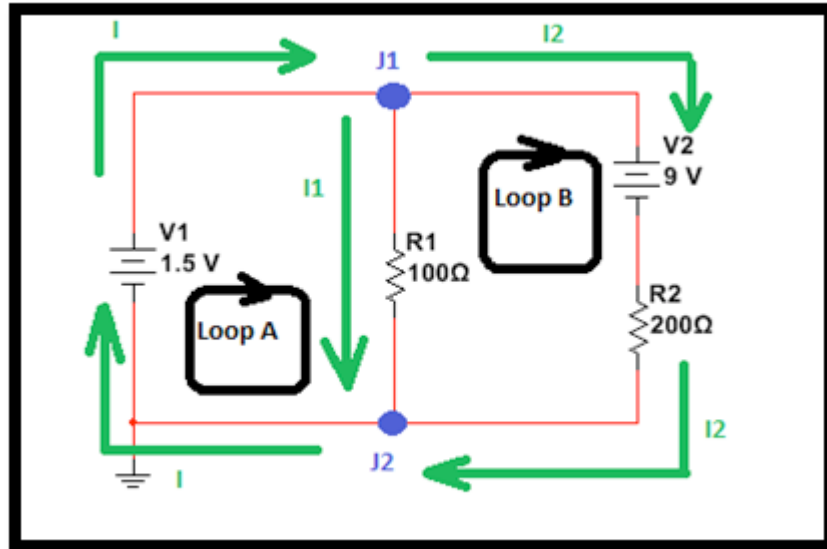
$$I = I_1 + I_2 \text{ (equation 1)}$$

Junction J_2 :

$I_1 + I_2 = I$ (which is the exact same equation we got from J_1 above)

Determine the voltage drops V_{R1} and V_{R2} across each resistor.

Begin by labelling the loops as loop **A** and loop **B** as shown below.



Loop A: (start from the upper left corner and move clockwise)

$$-I_1 \times (100 \, \Omega) + 1.5V = 0 \text{ (equation 2)}$$

Therefore: $I_1 = 0.015 \text{ A}$

Loop B:

$$-9V - I_2 \times (200 \, \Omega) + I_1 \times (100 \, \Omega) = 0 \text{ (equation 3)}$$

Substituting the value of I_1 into equation 3 yields:

$$-9 - I_2 \times (200 \, \Omega) + (0.015)(100 \, \Omega) = 0$$

$$-7.5 = (200) \times I_2 \text{ therefore: } I_2 = -0.0375 \text{ A}$$

And then $I = -0.0225 \text{ A}$

Note that the negative sign of the current indicates that the arbitrary direction we chose is the opposite of the actual direction the current is flowing in.

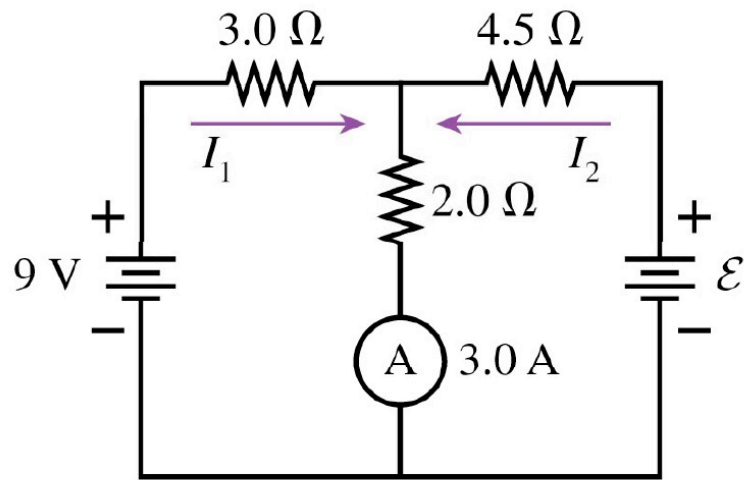
Answer Sub-Step 3: Determine the values of V_{R1} and V_{R2} based on our calculated values for I_1 and I_2

$$V_{R1} = I_1 \times R_1 = (0.015 \text{ A}) \times (100 \, \Omega) \text{ therefore } V_{R1} = 1.5V$$

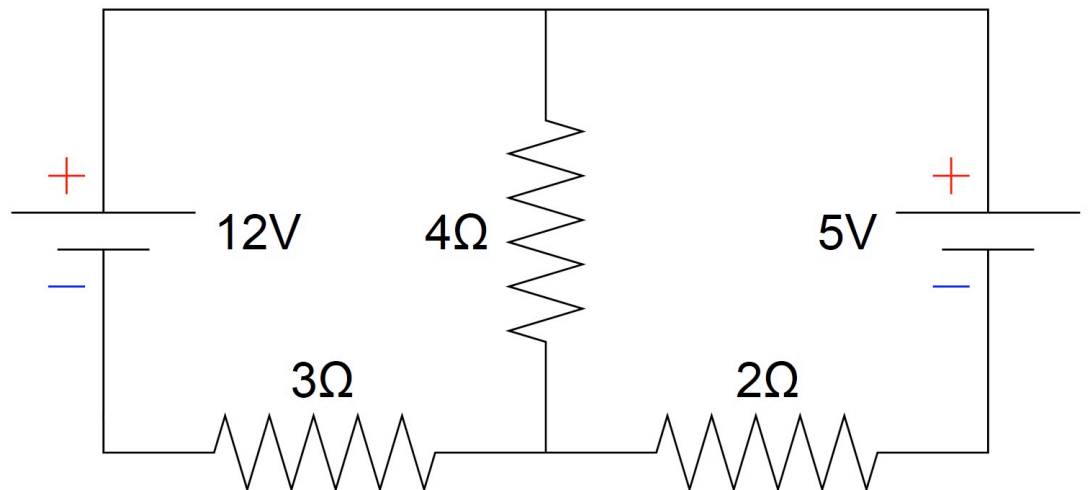
$$V_{R2} = I_2 \times R_2 = (-0.0375 \text{ A}) \times (200 \, \Omega) \text{ therefore } V_{R2} = -7.5V$$

Find all the currents and voltages across each resistor and cell in the following circuits;

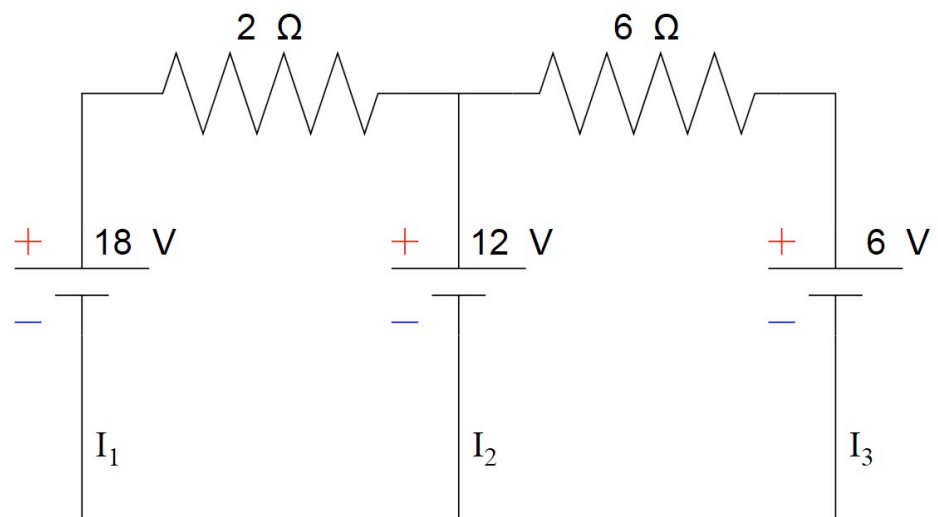
1.



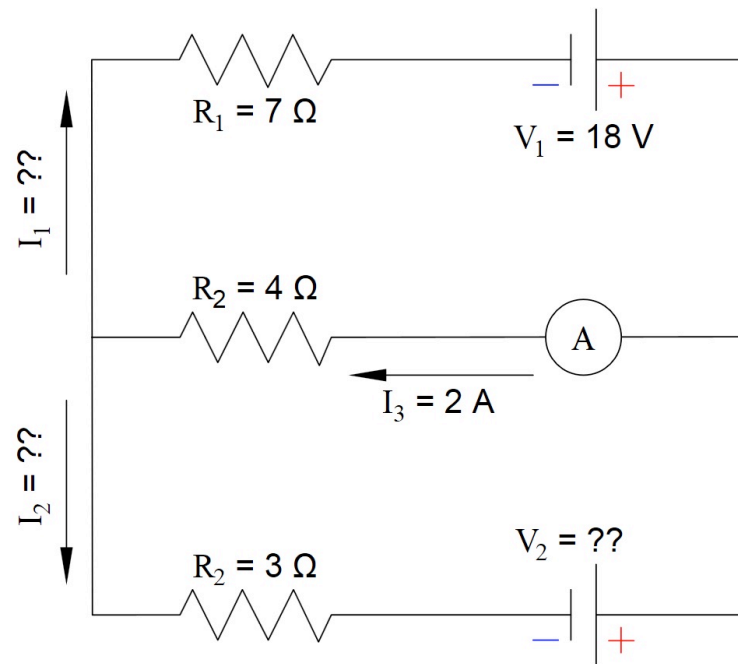
2.



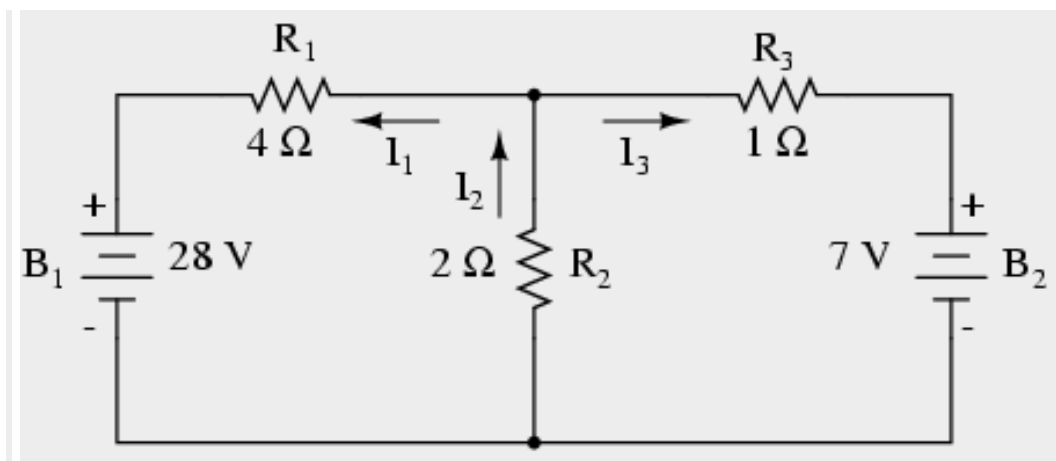
3.



4.



5.



6.

